

# Tentamen Structuur der Materie

March 31, 2014

## Opgave 1

- a)  $l = 0, 1, 2, n - 1 \rightarrow l = 0, 1, 2, 3, 4$
- b) see p.77,  $\cos \theta = \frac{m_l}{\sqrt{l(l+1)}}$
- c) Use  $n = l + \nu + 1$ , such that we have  $\nu = 4$  and  $1$  (number of nodes) for the 5s and 5f states, respectively. Draw this with the correct zero crossings, always starting positive, the maximum is always far away from the nucleus ( $r=0$ ) and it goes to zero exponentially. See p.80
- d)  $E_n = \frac{-13.6\text{eV}}{n^2}$  p.77
- e) States with higher angular momentum are affected most by the repulsive centrifugal force, pushed further from the nucleus and are less tightly bound.

## Opgave 2

- a) Strong, weak and electromagnetic interaction
- b) gluon, W/Z bosons and photon, respectively
- c)  $< 10^{-22}$  s,  $10^{-14} - 10^{-20}$ s,  $10^{-8} - 10^{-13}$  s respectively.
- d)  $Q = -1$
- e)  $Y = -1$  (see p.357)
- f)  $I_3 = -1/2$
- g) Baryon number conserved. Lepton number conserved.  $\Delta S = 1$ , so not allowed

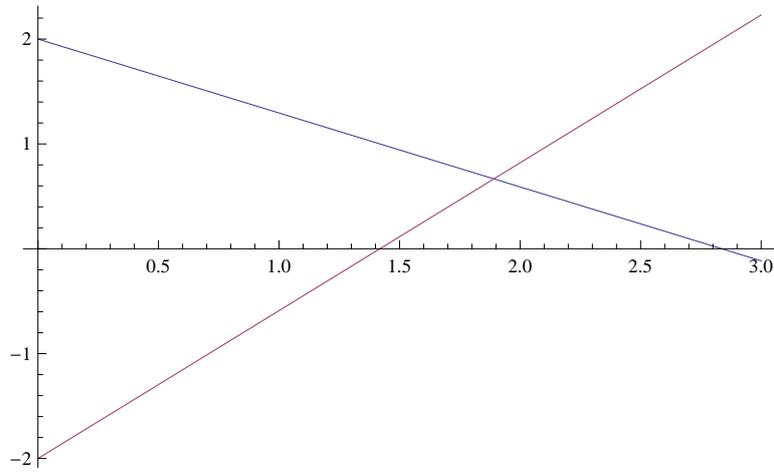
h) Strangeness changing is allowed by the weak interaction.

### Opgave 3

- a) 22 electrons:  $1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^2$
- b)  $3d^2$ , so two equivalent electrons with  $s_1 = s_2 = 1/2$  and  $l_1 = l_2 = 2$ , this couples to  $S = 0, 1$  and  $L = 0, 1, 2, 3, 4$ . Equivalent electrons so  $L + S = \text{even}$ .  $^1S_0, ^3P_{0,1,2}, ^1D_2, ^3F_{2,3,4}, ^1G_4$
- c)  $^3F_2$
- d)  $R = 1.12A^{1/3}$  fm, so  $A=47$ , gives  $R=4$  fm
- e)  $\frac{22e}{4/3\pi R^3} = 0.08e/\text{fm}^3$
- f) see p.410: 22 protonen,  $1s_{1/2}1p_{3/2}1p_{1/2}1d_{5/2}2s_{1/2}1d_{3/2}1f_{7/2}$   
25 neutronen:  $1s_{1/2}1p_{3/2}1p_{1/2}1d_{5/2}2s_{1/2}1d_{3/2}1f_{7/2}$
- g)  $J = 7/2$  from previous question,  $P = (-1)^L$  with  $L=3$

### Opgave 4

- a)  $2S + 1 = 3$ , so  $S = 1$  and  $L = 1$ ,  $J = |L - S|, \dots, |L + S| = 0, 1, 2$
- b) see figure 4.18. Use formula for  $E_{SO}$ , to find that the energy is  $-2B_{SO}, -B_{SO}, B_{SO}$  for  $J = 0, 1, 2$  respectively. So the  $^3P$  term is in between the  $J = 2$  and  $J = 1$  energies.
- c) For this we need the multiplicity  $(2J+1)$  of the terms, such that we get  $5 \times B + 3 \times -B + 1 \times -2B = 0$ , so there is indeed no shift and the total binding energy is equal to the energy of the  $^3P$  term.
- d) In this case the ground level is the  $J = 2$  level, because  $B$  is negative. Using Hund's rules we know that the highest  $J$  level is the ground state if the shell is more than half filled. So this is term belongs to O.
- e) We now get the  $m_J = -J, \dots, J$  values, which split linearly in a magnetic field with the highest  $m_J$  above. See p.101.
- f) The weak field approximation breaks down if two levels cross. This would happen first with the  $J=2$  and  $m_J = 2$  and the  $J=1$   $m_J = -1$  levels. For the running (steepness of the slope) we have to calculate the  $g_J$



values. Both have  $g_J = 3/2$ . in the weak field the energy goes like (see p.101)  $E = g_J \mu_B B m_J$ . We now need to solve  $-2\text{cm}^{-1} + 3/2 \mu_B B 1 = 2\text{cm}^{-1} - 3/2 \mu_B B 2$ , which gives  $B = 1.9T$ . See also the plot below, where the red curve is the  $m_J = 2$  of the  $J=2$  and the blue is the  $m_J = -1$  of the  $J = 1$ .